



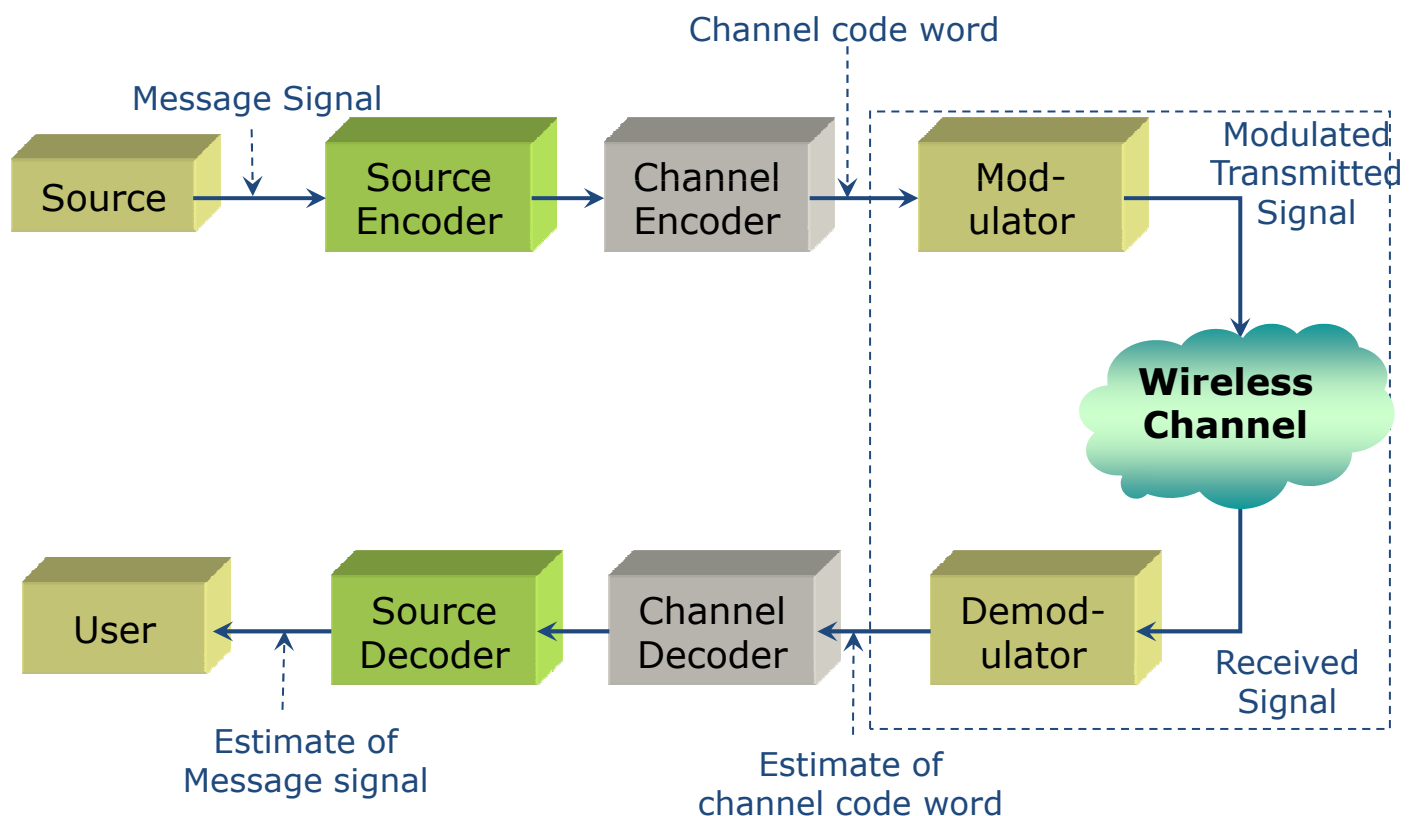
**UNIVERSITAS KOMPUTER  
INDONESIA**

## Wireless and Mobile Communication

### Chap 4 Antennas & Propagation Signal Encoding

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# Wireless Communication System



# Introduction

- An antenna is an electrical conductor or system of conductors
  - Transmission - radiates electromagnetic energy into space
  - Reception - collects electromagnetic energy from space
- In two-way communication, the same antenna can be used for transmission and reception

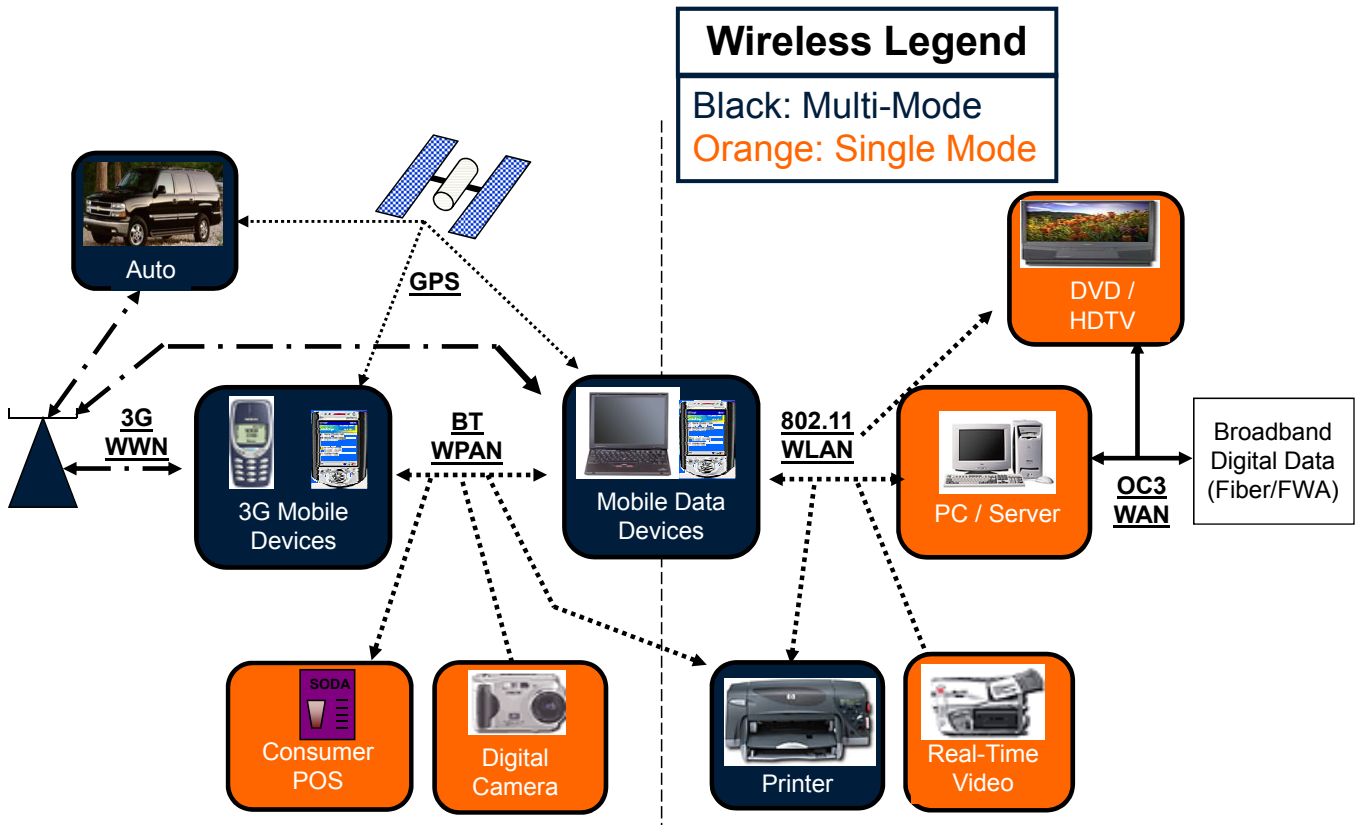


## Antenna Evolution

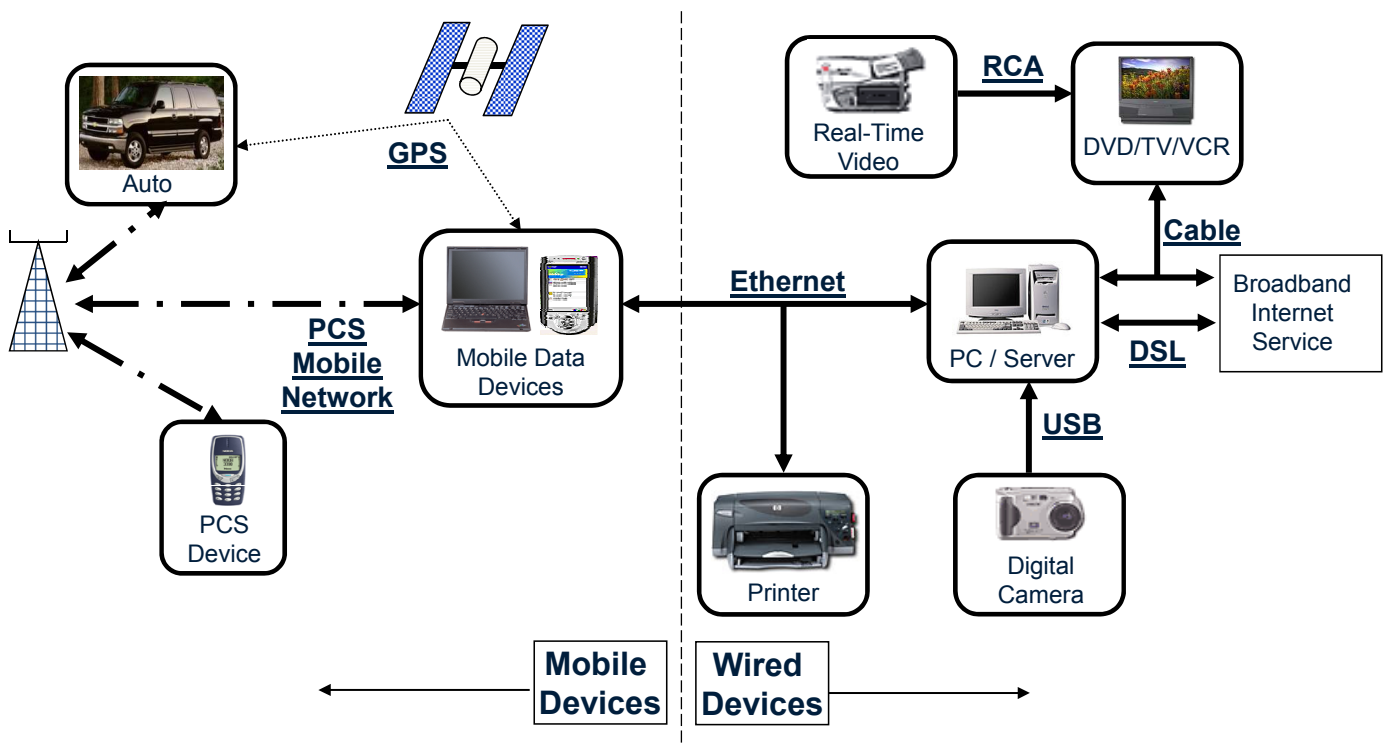
- Antennas Have Always Been the Part That Makes a Wireless Device Wireless
- Have Traditionally Been External, Connectorized Components
  - Misunderstood, considered “*black magic*”
  - Gangly, obtrusive
  - Added on at the end of the design
- Antennas for Mobile Devices Have Evolved Since Their Introduction
  - Whips → Retractable → Stubbies → Embedded



# Future of the Wired/Wireless World

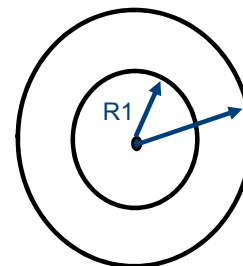


# Wired/Wireless Networks of Today

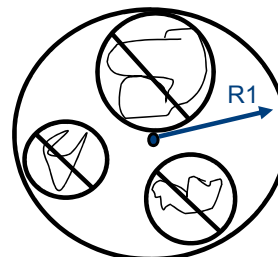


# Antenna Performance

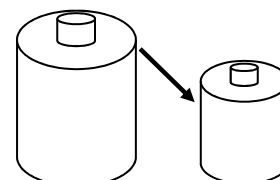
- Better Performance is Usually Achieved by Increased S/N in the Wireless Link
  - Performance improvements can be realized by higher gain antenna (if beam is properly focused)
    - Example: Want horizontal beam for cell phone, zenith beam for GPS
- Increased Gain Can be Used in Different Ways
  - Better cell coverage area
    - Increase cell size / range
    - Given all mobiles at max power, then less dropouts
  - Less battery power
    - Given strong signal area, then reduced Tx Battery
    - Especially critical in CDMA networks
  - Some combination of above



Increase Cell Coverage



Reduce Dropouts



Reduce Battery Size



## THEORY OF ANTENNA



# Radiation Patterns

- Radiation pattern
  - Graphical representation of radiation properties of an antenna
  - Depicted as two-dimensional cross section
- Beam width (or half-power beam width)
  - Measure of directivity of antenna
  - Angle within which power radiated is at least half of that in most preferred direction
- Reception pattern
  - Receiving antenna's equivalent to radiation pattern
- Omnidirectional vs. directional antenna

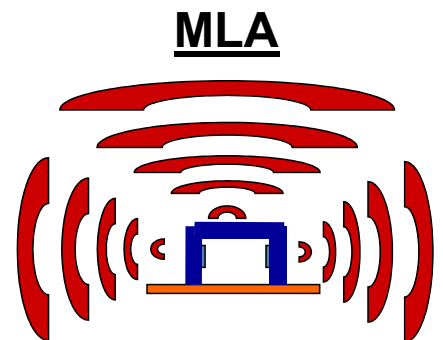
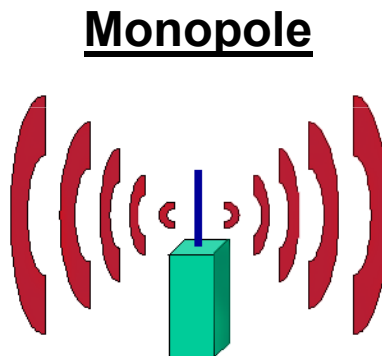
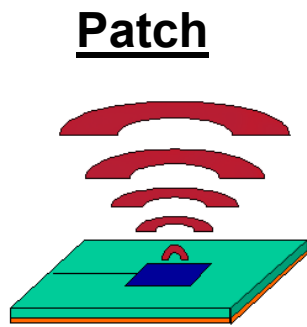
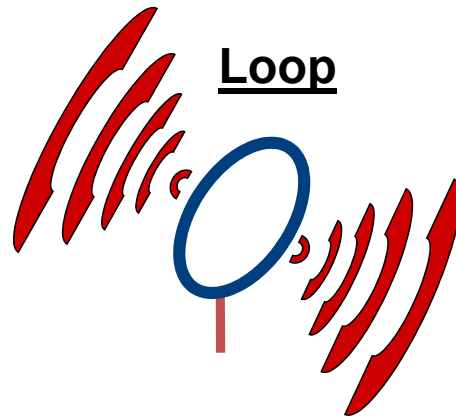
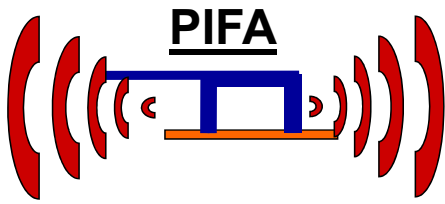


# Types of Antennas

- Isotropic antenna (idealized)
  - Radiates power equally in all directions
- Dipole antennas
  - Half-wave dipole antenna (or Hertz antenna)
  - Quarter-wave vertical antenna (or Marconi antenna)
- Parabolic Reflective Antenna
  - Used for terrestrial microwave and satellite applications
  - Larger the diameter, the more tightly directional is the beam

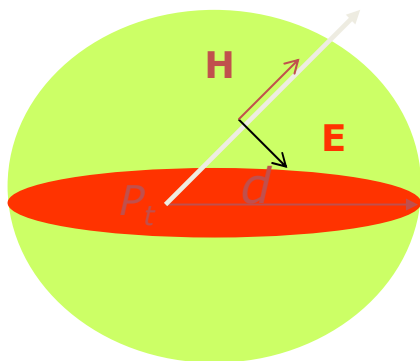


# Wireless Device Antenna Choices

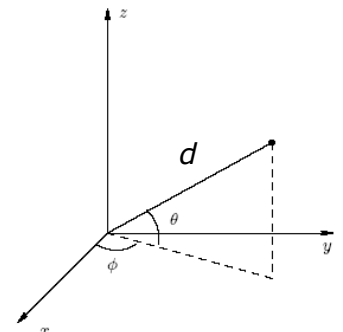


## Antenna - Ideal

- Isotropics antenna: In free space radiates power equally in all direction. Not realizable physically



EM fields around a transmitting antenna, a polar coordinate



- $d$ - distance directly away from the antenna.
- $\phi$  is the azimuth, or angle in the horizontal plane.
- $\theta$  is the zenith, or angle above the horizon.



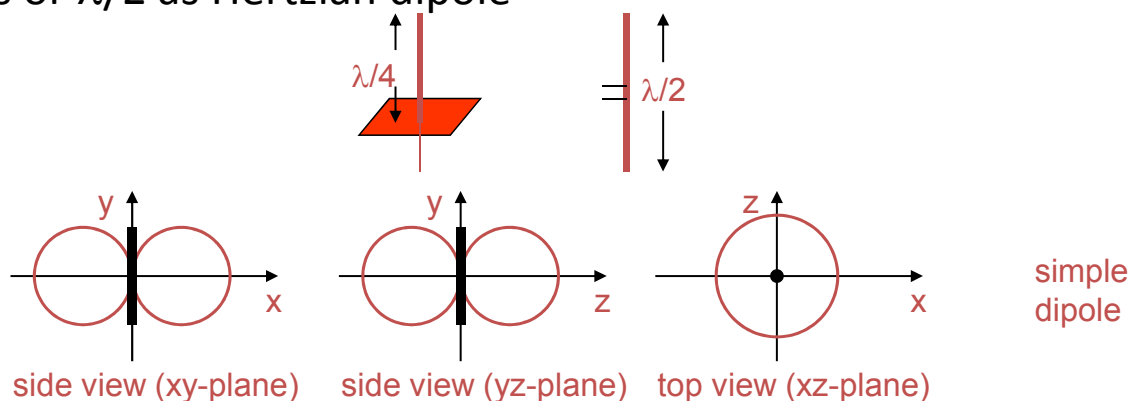
# Antenna - Real

- Not isotropic radiators, but always have directive effects (vertically and/or horizontally)
- A well defined radiation pattern measured around an antenna
- Patterns are visualised by drawing the set of constant-intensity surfaces



## Antenna – Real - Simple Dipoles

- Not isotropic radiators, e.g., dipoles with lengths  $\lambda/4$  on car roofs or  $\lambda/2$  as Hertzian dipole

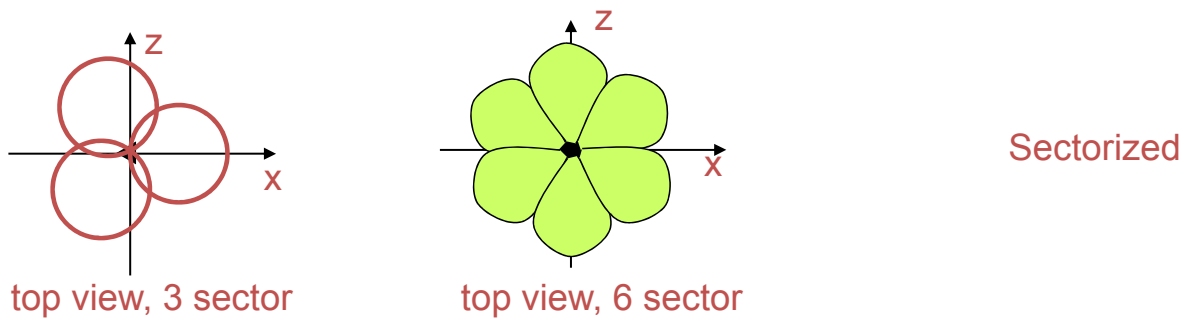
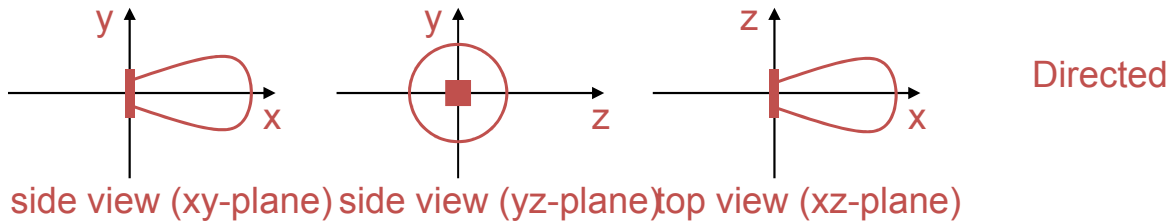


- Example: Radiation pattern of a simple Hertzian dipole  
shape of antenna is proportional to the wavelength



# Antenna – Real - **S**directed and **S**ectorized

- Used for microwave or base stations for mobile phones (e.g., radio coverage of a valley)



## Antenna Gain

- Antenna gain
  - Power output, in a particular direction, compared to that produced in any direction by a perfect omnidirectional antenna (isotropic antenna)
- Expressed in terms of effective area
  - Related to physical size and shape of antenna



# Antenna Gain

- Relationship between antenna gain and effective area

$$G = \frac{4\pi A_e}{\lambda^2} = \frac{4\pi f^2 A_e}{c^2}$$

- $G$  = antenna gain
- $A_e$  = effective area
- $f$  = carrier frequency
- $c$  = speed of light ( $\approx 3 \times 10^8$  m/s)
- $\lambda$  = carrier wavelength



## Antenna - Ideal - contd.

- The power density of an ideal loss-less antenna at a distance  $d$  away from the transmitting antenna:

$$P_a = \frac{P_t G_t}{4\pi d^2} \quad \text{W/m}^2$$

Note: the area is for a sphere.

- $G_t$  is the transmitting antenna gain
- The product  $P_t G_t$  : **Equivalent Isotropic Radiation Power (EIRP)**

which is the power fed to a perfect isotropic antenna to get the same output power of the practical antenna in hand.



## Antenna - Ideal - contd.

- The strength of the signal is often defined in terms of its Electric Field Intensity  $E$ , because it is easier to measure.

$P_a = E^2/R_m$  where  $R_m$  is the impedance of the medium. For free space  $R_m = 377$  Ohms.

$$E^2 = \frac{P_t R_m}{4\pi d^2} \quad \text{and} \quad E = \sqrt{\frac{P_t R_m}{4\pi d^2}} \quad \text{V/m}$$



## Antenna - Ideal - contd.

- The receiving antenna is characterized by its effective aperture  $A_e$ , which describes how well an antenna can pick up power from an incoming electromagnetic wave
- The effective aperture  $A_e$  is related to the gain  $G_r$  as follows:

$$A_e = P_r / P_a \Rightarrow A_e = G_r \lambda^2 / 4\pi$$

which is the equivalent power absorbing area of the antenna.

$G_r$  is the receiving antenna gain and  $\lambda = c/f$

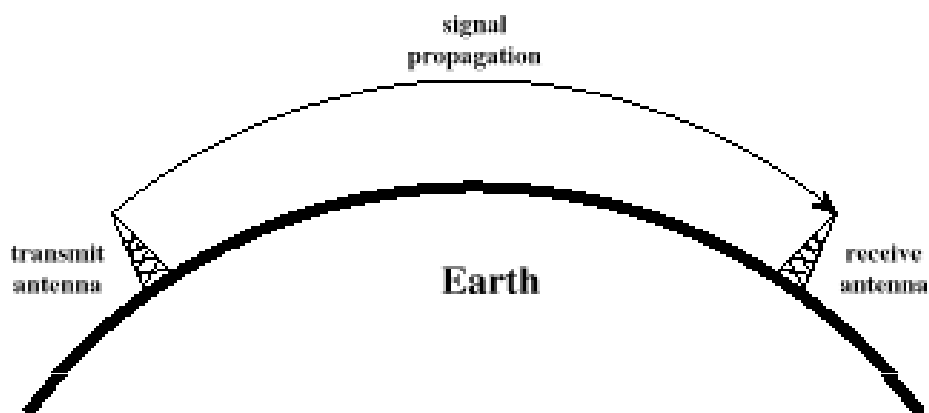


# Propagation Modes

- Ground-wave propagation
- Sky-wave propagation
- Line-of-sight propagation
- Non line of sight propagation



## Ground Wave Propagation

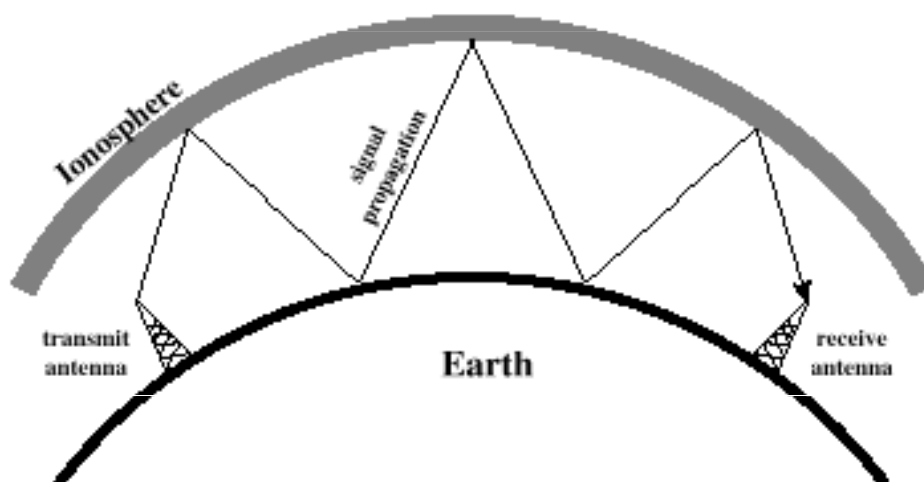


# Ground Wave Propagation

- Follows contour of the earth
- Can Propagate considerable distances
- Frequencies up to 2 MHz
- Example
  - AM radio



# Sky Wave Propagation

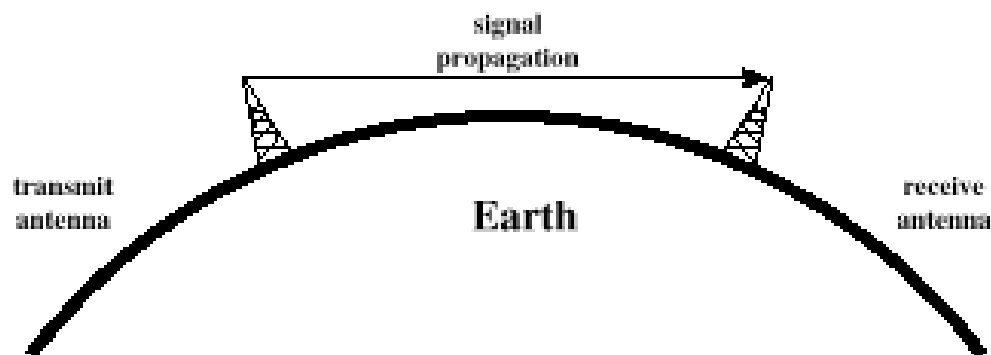


# Sky Wave Propagation

- Signal reflected from ionized layer of atmosphere back down to earth
- Signal can travel a number of hops, back and forth between ionosphere and earth's surface
- Reflection effect caused by refraction
- Examples
  - Amateur radio
  - CB radio

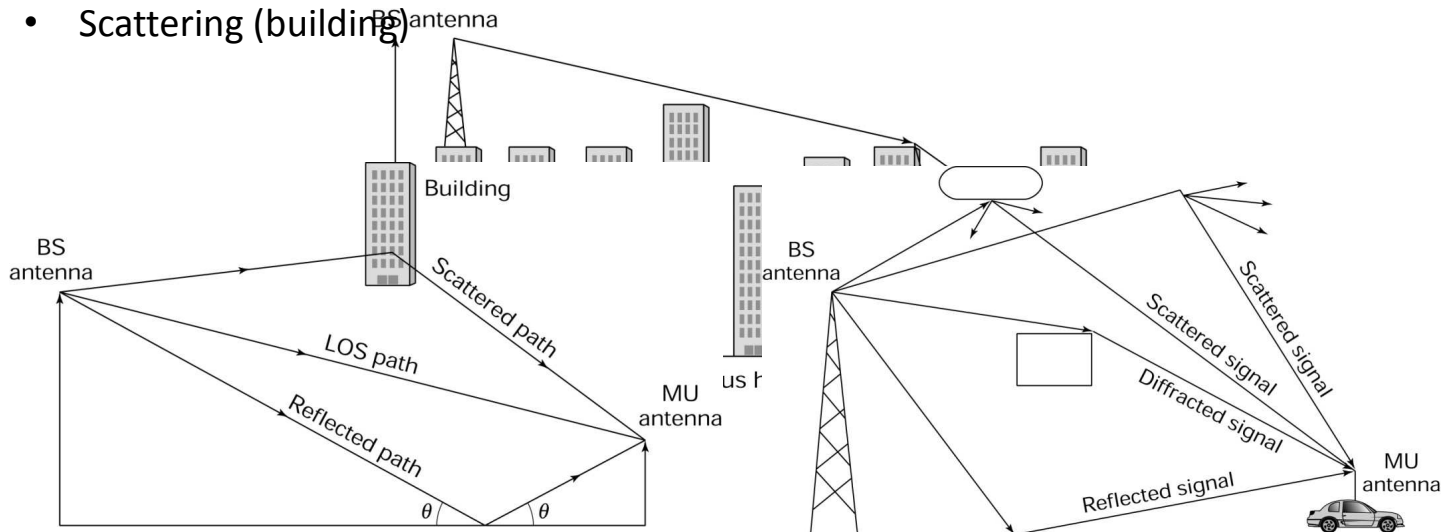


# Line-of-Sight Propagation



# Propagation Non line of sight

- Reflection (rough terrain, moving vehicle)
- Diffraction (edge of Building)
- Scattering (building)



Source: P M Shankar



## Line-of-Sight Propagation

- Transmitting and receiving antennas must be within line of sight
  - Satellite communication – signal above 30 MHz not reflected by ionosphere
  - Ground communication – antennas within *effective* line of site due to refraction
- Refraction – bending of microwaves by the atmosphere
  - Velocity of electromagnetic wave is a function of the density of the medium
  - When wave changes medium, speed changes
  - Wave bends at the boundary between mediums



# Line-of-Sight Equations

- Optical line of sight

$$d = 3.57\sqrt{h}$$

- Effective, or radio, line of sight

$$d = 3.57\sqrt{Kh}$$

- $d$  = distance between antenna and horizon (km)
- $h$  = antenna height (m)
- $K$  = adjustment factor to account for refraction, rule of thumb  $K = 4/3$



# Line-of-Sight Equations

- Maximum distance between two antennas for LOS propagation:

$$3.57\left(\sqrt{Kh_1} + \sqrt{Kh_2}\right)$$

- $h_1$  = height of antenna one
- $h_2$  = height of antenna two



# LOS Wireless Transmission Impairments

- Attenuation and attenuation distortion
- Free space loss
- Noise
- Atmospheric absorption
- Multipath
- Refraction
- Thermal noise



## Attenuation

- Strength of signal falls off with distance over transmission medium
- Attenuation factors for unguided media:
  - Received signal must have sufficient strength so that circuitry in the receiver can interpret the signal
  - Signal must maintain a level sufficiently higher than noise to be received without error
  - Attenuation is greater at higher frequencies, causing distortion





# Free Space Loss

- Free space loss, ideal isotropic antenna

$$\frac{P_t}{P_r} = \frac{(4\pi d)^2}{\lambda^2} = \frac{(4\pi f d)^2}{c^2}$$

- $P_t$  = signal power at transmitting antenna
  - $P_r$  = signal power at receiving antenna
  - $\lambda$  = carrier wavelength
  - $d$  = propagation distance between antennas
  - $c$  = speed of light ( $\approx 3 \times 10^8$  m/s)
- where  $d$  and  $\lambda$  are in the same units (e.g., meters)



# Free Space Loss

- Free space loss equation can be recast:

$$\begin{aligned} L_{dB} &= 10 \log \frac{P_t}{P_r} = 20 \log \left( \frac{4\pi d}{\lambda} \right) \\ &= -20 \log(\lambda) + 20 \log(d) + 21.98 \text{ dB} \\ &= 20 \log \left( \frac{4\pi f d}{c} \right) = 20 \log(f) + 20 \log(d) - 147.56 \text{ dB} \end{aligned}$$



# Free Space Loss

- Free space loss accounting for gain of antennas

$$\frac{P_t}{P_r} = \frac{(4\pi)^2 (d)^2}{G_r G_t \lambda^2} = \frac{(\lambda d)^2}{A_r A_t} = \frac{(cd)^2}{f^2 A_r A_t}$$

- $G_t$  = gain of transmitting antenna
- $G_r$  = gain of receiving antenna
- $A_t$  = effective area of transmitting antenna
- $A_r$  = effective area of receiving antenna



# Free Space Loss

- Free space loss accounting for gain of other antennas can be recast as

$$\begin{aligned} L_{dB} &= 20\log(\lambda) + 20\log(d) - 10\log(A_t A_r) \\ &= -20\log(f) + 20\log(d) - 10\log(A_t A_r) + 169.54\text{dB} \end{aligned}$$



# Categories of Noise

- Thermal Noise
- Intermodulation noise
- Crosstalk
- Impulse Noise



## Thermal Noise

- Thermal noise due to agitation of electrons
- Present in all electronic devices and transmission media
- Cannot be eliminated
- Function of temperature
- Particularly significant for satellite communication



# Thermal Noise

- Amount of thermal noise to be found in a bandwidth of 1Hz in any device or conductor is:

$$N_0 = kT \text{ (W/Hz)}$$

- $N_0$  = noise power density in watts per 1 Hz of bandwidth
- $k$  = Boltzmann's constant =  $1.3803 \times 10^{-23}$  J/K
- $T$  = temperature, in kelvins (absolute temperature)



# Thermal Noise

- Noise is assumed to be independent of frequency
- Thermal noise present in a bandwidth of  $B$  Hertz (in watts):

$$N = kTB$$

or, in decibel-watts

$$\begin{aligned} N &= 10 \log k + 10 \log T + 10 \log B \\ &= -228.6 \text{ dBW} + 10 \log T + 10 \log B \end{aligned}$$



# Noise Terminology

- Intermodulation noise – occurs if signals with different frequencies share the same medium
  - Interference caused by a signal produced at a frequency that is the sum or difference of original frequencies
- Crosstalk – unwanted coupling between signal paths
- Impulse noise – irregular pulses or noise spikes
  - Short duration and of relatively high amplitude
  - Caused by external electromagnetic disturbances, or faults and flaws in the communications system
  - Primary source of error for digital data transmission



## Expression $E_b/N_0$

- Ratio of signal energy per bit to noise power density per Hertz

$$\frac{E_b}{N_0} = \frac{S/R}{N_0} = \frac{S}{kTR}$$

- The bit error rate for digital data is a function of  $E_b/N_0$ 
  - Given a value for  $E_b/N_0$  to achieve a desired error rate, parameters of this formula can be selected
  - As bit rate  $R$  increases, transmitted signal power must increase to maintain required  $E_b/N_0$



# Other Impairments

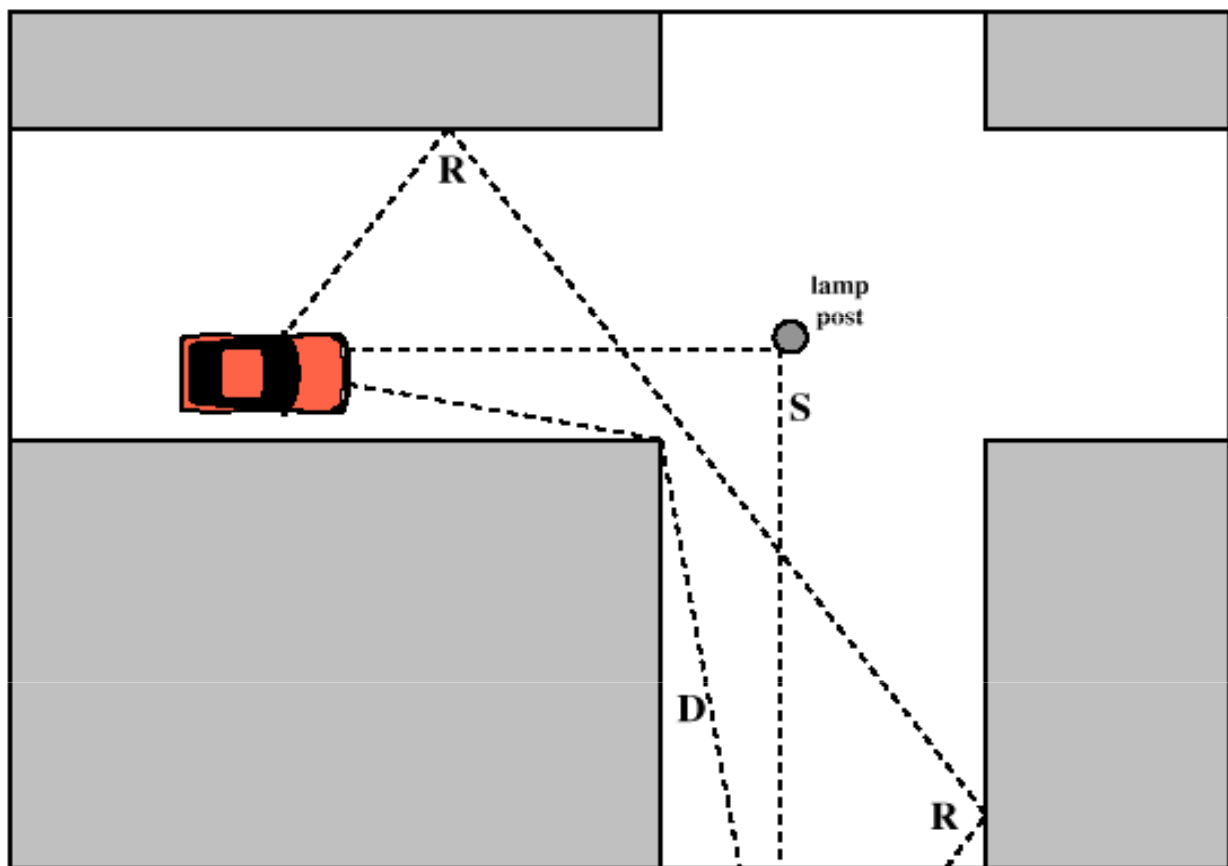
- Atmospheric absorption – water vapor and oxygen contribute to attenuation
- Multipath – obstacles reflect signals so that multiple copies with varying delays are received
- Refraction – bending of radio waves as they propagate through the atmosphere



# Multipath Propagation

- Reflection - occurs when signal encounters a surface that is large relative to the wavelength of the signal
- Diffraction - occurs at the edge of an impenetrable body that is large compared to wavelength of radio wave
- Scattering – occurs when incoming signal hits an object whose size is in the order of the wavelength of the signal or less





**Figure 5.10 Sketch of Three Important Propagation Mechanisms: Reflection (R), Scattering (S), Diffraction (D) [ANDE95]**

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## Effects of Multipath Propagation

- Multiple copies of a signal may arrive at different phases
  - If phases add destructively, the signal level relative to noise declines, making detection more difficult
- Intersymbol interference (ISI)
  - One or more delayed copies of a pulse may arrive at the same time as the primary pulse for a subsequent bit

# Fading

- Time variation of received signal power caused by changes in the transmission medium or path(s)
- In a fixed environment:
  - Changes in atmospheric conditions
- In a mobile environment:
  - Multipath propagation



## Types of Fading

- Fast fading
- Slow fading
- Flat fading
- Selective fading
- Rayleigh fading
- Rician fading





# Error Compensation Mechanisms

- Forward error correction
- Adaptive equalization
- Diversity techniques



## Forward Error Correction

- Transmitter adds error-correcting code to data block
  - Code is a function of the data bits
- Receiver calculates error-correcting code from incoming data bits
  - If calculated code matches incoming code, no error occurred
  - If error-correcting codes don't match, receiver attempts to determine bits in error and correct



# Adaptive Equalization

- Can be applied to transmissions that carry analog or digital information
  - Analog voice or video
  - Digital data, digitized voice or video
- Used to combat intersymbol interference
- Involves gathering dispersed symbol energy back into its original time interval
- Techniques
  - Lumped analog circuits
  - Sophisticated digital signal processing algorithms



# Diversity Techniques

- Space diversity:
  - Use multiple nearby antennas and combine received signals to obtain the desired signal
  - Use collocated multiple directional antennas
- Frequency diversity:
  - Spreading out signal over a larger frequency bandwidth
  - Spread spectrum
- Time diversity:
  - Noise often occurs in bursts
  - Spreading the data out over time spreads the errors and hence allows FEC techniques to work well
  - TDM
  - Interleaving



# Signal Encoding Techniques



## Reasons for Choosing Encoding Techniques

- Digital data, digital signal
  - Equipment less complex and expensive than digital-to-analog modulation equipment
- Analog data, digital signal
  - Permits use of modern digital transmission and switching equipment



# Reasons for Choosing Encoding Techniques

- Digital data, analog signal
  - Some transmission media will only propagate analog signals
  - E.g., unguided media
- Analog data, analog signal
  - Analog data in electrical form can be transmitted easily and cheaply
  - Done with voice transmission over voice-grade lines



## Signal Encoding Criteria

- What determines how successful a receiver will be in interpreting an incoming signal?
  - Signal-to-noise ratio
  - Data rate
  - Bandwidth
- An increase in data rate increases bit error rate
- An increase in SNR decreases bit error rate
- An increase in bandwidth allows an increase in data rate



# Comparing Encoding Schemes

- Signal spectrum
  - With lack of high-frequency components, less bandwidth required
  - With no dc component, ac coupling via transformer possible
  - Transfer function of a channel is worse near band edges
- Clocking
  - Ease of determining beginning and end of each bit position



# Comparing Encoding Schemes

- Signal interference and noise immunity
  - Performance in the presence of noise
- Cost and complexity
  - The higher the signal rate to achieve a given data rate, the greater the cost



# Digital Data to Analog Signals

- Amplitude-shift keying (ASK)
  - Amplitude difference of carrier frequency
- Frequency-shift keying (FSK)
  - Frequency difference near carrier frequency
- Phase-shift keying (PSK)
  - Phase of carrier signal shifted

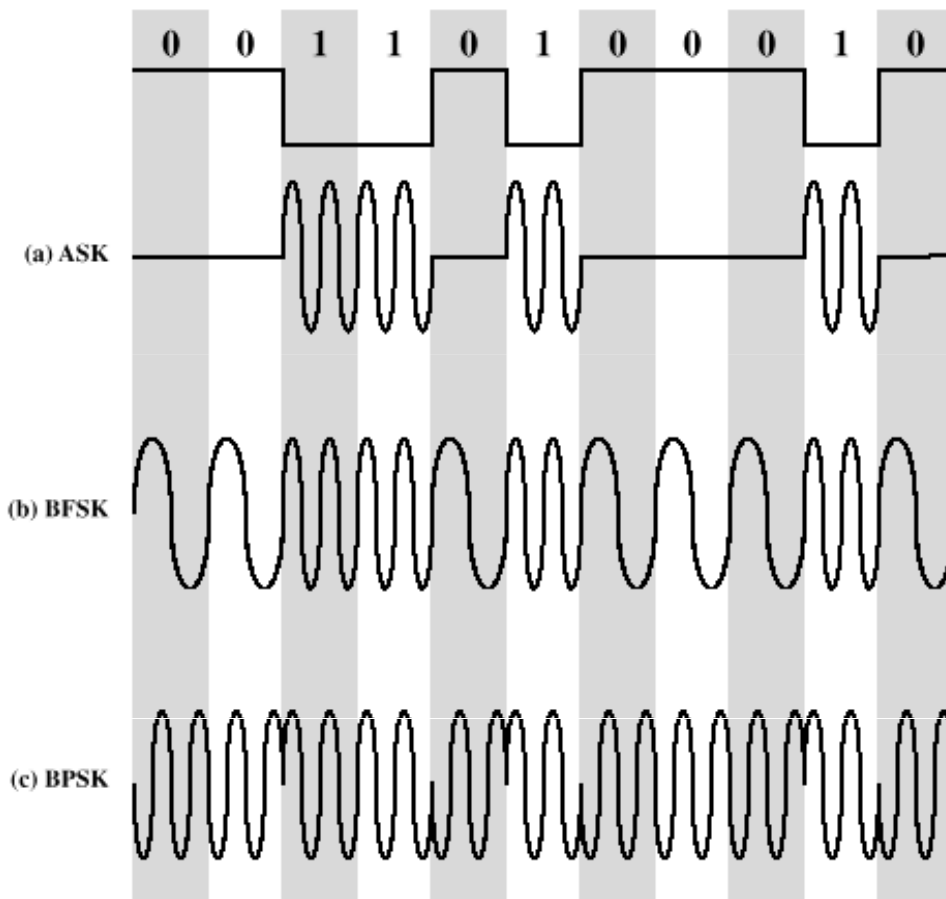


Figure 6.2 Modulation of Analog Signals for Digital Data

# Amplitude-Shift Keying

- One binary digit represented by presence of carrier, at constant amplitude
- Other binary digit represented by absence of carrier

$$s(t) = \begin{cases} A \cos(2\pi f_c t) & \text{binary 1} \\ 0 & \text{binary 0} \end{cases}$$

- where the carrier signal is  $A \cos(2\pi f_c t)$



# Amplitude-Shift Keying

- Susceptible to sudden gain changes
- Inefficient modulation technique
- On voice-grade lines, used up to 1200 bps
- Used to transmit digital data over optical fiber



# Binary Frequency-Shift Keying (BFSK)

- Two binary digits represented by two different frequencies near the carrier frequency

$$s(t) = \begin{cases} A \cos(2\pi f_1 t) & \text{binary 1} \\ A \cos(2\pi f_2 t) & \text{binary 0} \end{cases}$$

- where  $f_1$  and  $f_2$  are offset from carrier frequency  $f_c$  by equal but opposite amounts



# Binary Frequency-Shift Keying (BFSK)

- Less susceptible to error than ASK
- On voice-grade lines, used up to 1200bps
- Used for high-frequency (3 to 30 MHz) radio transmission
- Can be used at higher frequencies on LANs that use coaxial cable





# Multiple Frequency-Shift Keying (MFSK)

- More than two frequencies are used
- More bandwidth efficient but more susceptible to error

$$s_i(t) = A \cos 2\pi f_i t \quad 1 \leq i \leq M$$

- $f_i = f_c + (2i - 1 - M)f_d$
- $f_c$  = the carrier frequency
- $f_d$  = the difference frequency
- $M$  = number of different signal elements =  $2^L$
- $L$  = number of bits per signal element



# Multiple Frequency-Shift Keying (MFSK)

- To match data rate of input bit stream, each output signal element is held for:

$$T_s = LT \text{ seconds}$$

- where  $T$  is the bit period (data rate =  $1/T$ )
- So, one signal element encodes  $L$  bits



# Multiple Frequency-Shift Keying (MFSK)

- Total bandwidth required

$$2Mf_d$$

- Minimum frequency separation required

$$2f_d = 1/T_s$$

- Therefore, modulator requires a bandwidth of

$$W_d = 2^L/LT = M/T_s$$



# Multiple Frequency-Shift Keying (MFSK)

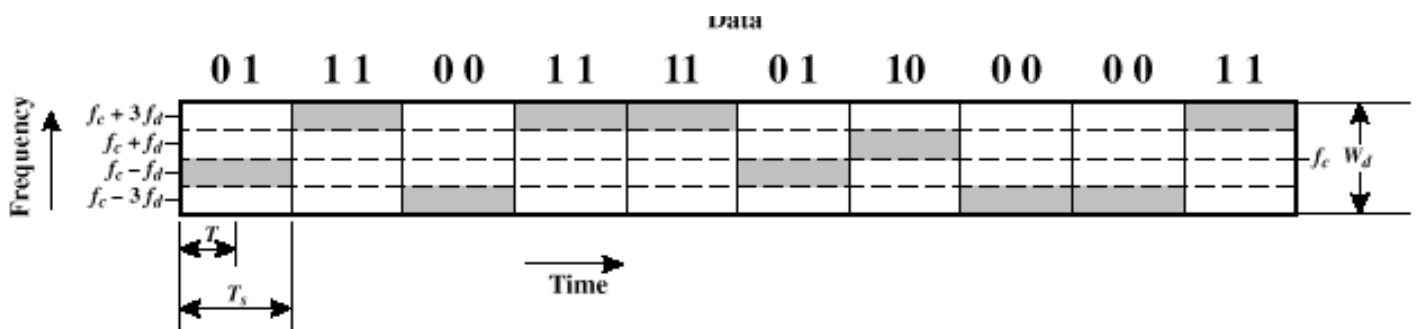


Figure 6.4 MFSK Frequency Use ( $M = 4$ )



# Phase-Shift Keying (PSK)

- Two-level PSK (BPSK)
  - Uses two phases to represent binary digits

$$s(t) = \begin{cases} A \cos(2\pi f_c t) & \text{binary 1} \\ A \cos(2\pi f_c t + \pi) & \text{binary 0} \end{cases}$$
$$= \begin{cases} A \cos(2\pi f_c t) & \text{binary 1} \\ -A \cos(2\pi f_c t) & \text{binary 0} \end{cases}$$



# Phase-Shift Keying (PSK)

- Differential PSK (DPSK)
  - Phase shift with reference to previous bit
    - Binary 0 – signal burst of same phase as previous signal burst
    - Binary 1 – signal burst of opposite phase to previous signal burst



# Phase-Shift Keying (PSK)

- Four-level PSK (QPSK)
  - Each element represents more than one bit

$$s(t) = \begin{cases} A \cos\left(2\pi f_c t + \frac{\pi}{4}\right) & 11 \\ A \cos\left(2\pi f_c t + \frac{3\pi}{4}\right) & 01 \\ A \cos\left(2\pi f_c t - \frac{3\pi}{4}\right) & 00 \\ A \cos\left(2\pi f_c t - \frac{\pi}{4}\right) & 10 \end{cases}$$



# Phase-Shift Keying (PSK)

- Multilevel PSK
  - Using multiple phase angles with each angle having more than one amplitude, multiple signals elements can be achieved

$$D = \frac{R}{L} = \frac{R}{\log_2 M}$$

- $D$  = modulation rate, baud
- $R$  = data rate, bps
- $M$  = number of different signal elements =  $2^L$
- $L$  = number of bits per signal element



# Performance

- Bandwidth of modulated signal ( $B_T$ )

- ASK, PSK  $B_T = (1+r)R$

- FSK  $B_T = 2DF + (1+r)R$

- $R$  = bit rate
    - $0 < r < 1$ ; related to how signal is filtered
    - $DF = f_2 - f_c = f_c - f_1$



# Performance

- Bandwidth of modulated signal ( $B_T$ )

- MPSK  $B_T = \left(\frac{1+r}{L}\right)R = \left(\frac{1+r}{\log_2 M}\right)R$

- MFSK  $B_T = \left(\frac{(1+r)M}{\log_2 M}\right)R$

- $L$  = number of bits encoded per signal element
    - $M$  = number of different signal elements



# Quadrature Amplitude Modulation

- QAM is a combination of ASK and PSK
  - Two different signals sent simultaneously on the same carrier frequency

$$s(t) = d_1(t)\cos 2\pi f_c t + d_2(t)\sin 2\pi f_c t$$

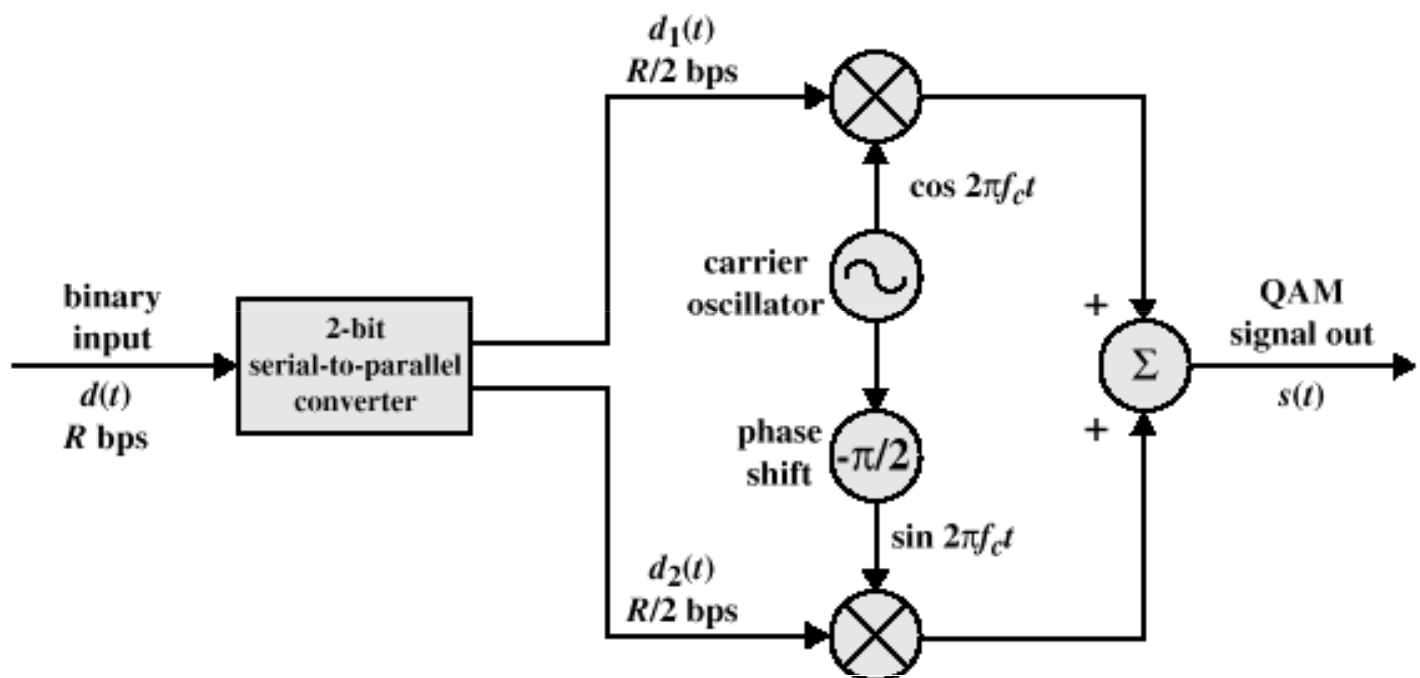


Figure 6.10 QAM Modulator

# Analog Data to Analog Signal

- Modulation of digital signals
  - When only analog transmission facilities are available, digital to analog conversion required
- Modulation of analog signals
  - A higher frequency may be needed for effective transmission
  - Modulation permits frequency division multiplexing



## Modulation Techniques

- Amplitude modulation (AM)
- Angle modulation
  - Frequency modulation (FM)
  - Phase modulation (PM)



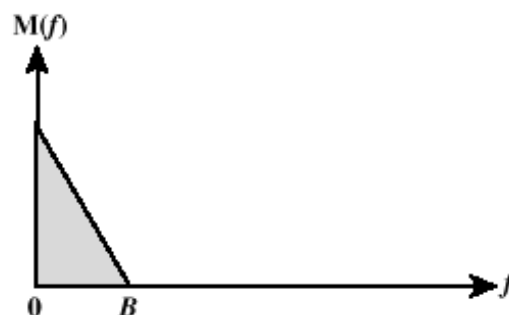
# Amplitude Modulation

- Amplitude Modulation

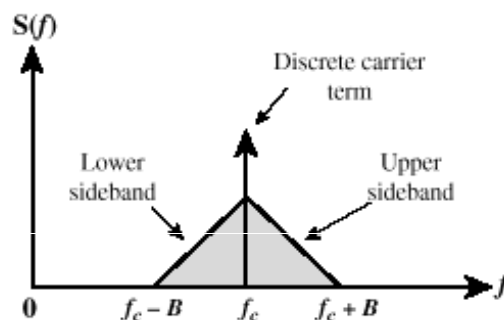
$$s(t) = [1 + n_a x(t)] \cos 2\pi f_c t$$

- $\cos 2\pi f_c t$  = carrier
- $x(t)$  = input signal
- $n_a$  = modulation index ( $< 1$ )
  - Ratio of amplitude of input signal to carrier

– a.k.a double sideband transmitted carrier (DSBTC)



(a) Spectrum of modulating signal



(b) Spectrum of AM signal with carrier at  $f_c$



# Amplitude Modulation

- Transmitted power

$$P_t = P_c \left( 1 + \frac{n_a^2}{2} \right)$$

- $P_t$  = total transmitted power in  $s(t)$
- $P_c$  = transmitted power in carrier



## Single Sideband (SSB)

- Variant of AM is single sideband (SSB)
  - Sends only one sideband
  - Eliminates other sideband and carrier
- Advantages
  - Only half the bandwidth is required
  - Less power is required
- Disadvantages
  - Suppressed carrier can't be used for synchronization purposes



# Angle Modulation

- Angle modulation

$$s(t) = A_c \cos[2\pi f_c t + \phi(t)]$$

- Phase modulation

– Phase is proportional to modulating signal

$$\phi(t) = n_p m(t)$$

- $n_p$  = phase modulation index



# Angle Modulation

- Frequency modulation

– Derivative of the phase is proportional to modulating signal

$$\phi'(t) = n_f m(t)$$

- $n_f$  = frequency modulation index



# Angle Modulation

- Compared to AM, FM and PM result in a signal whose bandwidth:
  - is also centered at  $f_c$
  - but has a magnitude that is much different
- Thus, FM and PM require greater bandwidth than AM



# Angle Modulation

- Carson's rule  $B_T = 2(\beta + 1)B$

where

$$\beta = \begin{cases} n_p A_m & \text{for PM} \\ \frac{\Delta F}{B} = \frac{n_f A_m}{2\pi B} & \text{for FM} \end{cases}$$

- The formula for FM becomes

$$B_T = 2\Delta F + 2B$$



# Analog Data to Digital Signal

- Digitization: Often analog data are converted to digital form
- Once analog data have been converted to digital signals, the digital data:
  - can be transmitted using NRZ-L
  - can be encoded as a digital signal using a code other than NRZ-L
  - can be converted to an analog signal, using previously discussed techniques



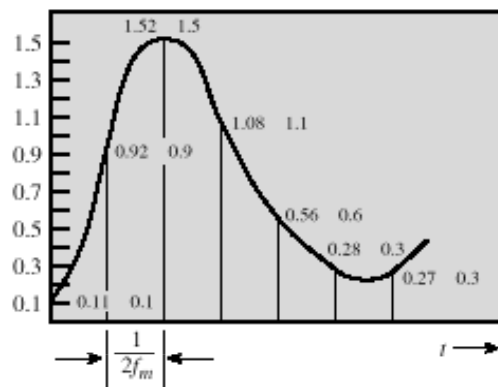
## Analog data to digital signal

- Pulse code modulation (PCM)
- Delta modulation (DM)



# Pulse Code Modulation

- Based on the sampling theorem
- Each analog sample is assigned a binary code
  - Analog samples are referred to as pulse amplitude modulation (PAM) samples
- The digital signal consists of block of  $n$  bits, where each  $n$ -bit number is the amplitude of a PCM pulse



(a)

Digit	Binary Equivalent	PCM waveform
0	0000	—
1	0001	—
2	0010	—
3	0011	—
4	0100	—
5	0101	—
6	0110	—
7	0111	—

Digit	Binary Equivalent	PCM waveform
8	1000	—
9	1001	—
10	1010	—
11	1011	—
12	1100	—
13	1101	—
14	1110	—
15	1111	—

(b)

**Figure 6.15 Pulse-Code Modulation**

# Pulse Code Modulation

- By quantizing the PAM pulse, original signal is only approximated
- Leads to quantizing noise
- Signal-to-noise ratio for quantizing noise
$$\text{SNR}_{\text{dB}} = 20 \log 2^n + 1.76 \text{ dB} = 6.02n + 1.76 \text{ dB}$$
- Thus, each additional bit increases SNR by 6 dB, or a factor of 4



# Delta Modulation

- Analog input is approximated by staircase function
  - Moves up or down by one quantization level ( $\delta$ ) at each sampling interval
- The bit stream approximates derivative of analog signal (rather than amplitude)
  - 1 is generated if function goes up
  - 0 otherwise



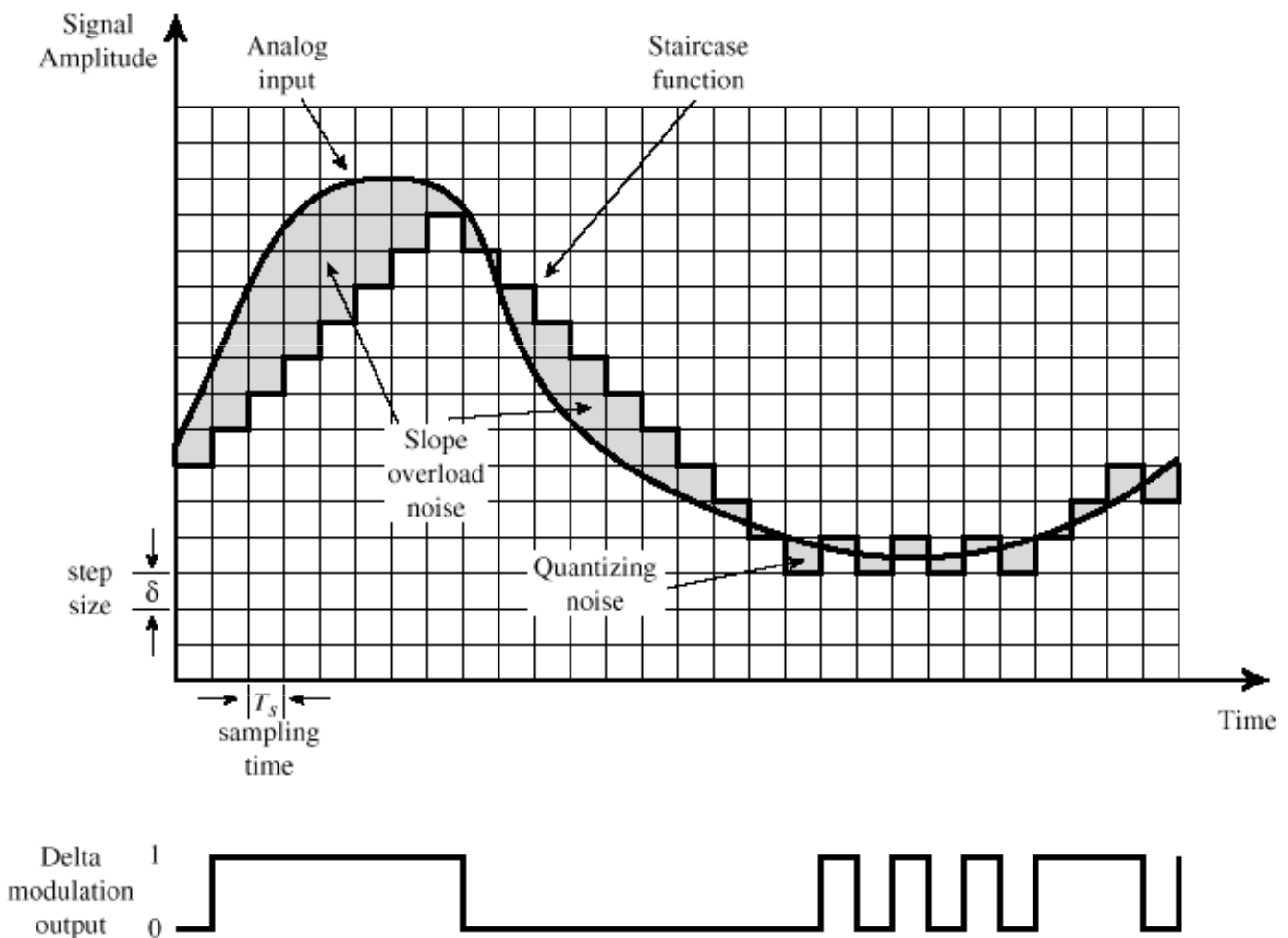


Figure 6.18 Example of Delta Modulation

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## Delta Modulation

- Two important parameters
  - Size of step assigned to each binary digit ( $\delta$ )
  - Sampling rate
- Accuracy improved by increasing sampling rate
  - However, this increases the data rate
- Advantage of DM over PCM is the simplicity of its implementation